

# Package ‘eigencore’

August 26, 2026

**Title** Certified Partial Eigenvalue and Singular Value Computation

**Version** 1.0.3

**Author** Bradley Buchsbaum [aut, cre, cph]

**Maintainer** Bradley Buchsbaum <brad.buchsbaum@gmail.com>

**Description** Computes the top-k singular triplets or eigenpairs of large sparse and structured matrices: the computation behind principal component analysis on big sparse data, spectral embeddings, and low-rank approximation. Every result carries a numerical certificate with residuals, a backward-error bound, orthogonality loss, and a pass/fail flag, and bounds that can only be estimated are reported as such rather than passed. Centered, scaled, and composed operators are solved through native 'C++' kernels without forming dense matrices. Drop-in replacements for the 'RSpectra' interface are included.

**URL** <https://bbuchsbaum.github.io/eigencore/>,  
<https://github.com/bbuchsbaum/eigencore>

**BugReports** <https://github.com/bbuchsbaum/eigencore/issues>

**License** MIT + file LICENSE

**Encoding** UTF-8

**RoxygenNote** 7.3.3

**Depends** R (>= 4.1)

**Imports** Matrix, methods

**Suggests** bench, knitr, rmarkdown, RSpectra, irlba, rsvd, testthat (>= 3.0.0)

**VignetteBuilder** knitr

**Config/testthat/edition** 3

**SystemRequirements** C++17

**Config/Needs/website** albersdown

**NeedsCompilation** yes

**Repository** CRAN

**Date/Publication** 2026-08-26 21:10:18 UTC

## Contents

|                                              |    |
|----------------------------------------------|----|
| adjoint . . . . .                            | 3  |
| alpha_beta . . . . .                         | 3  |
| as_operator . . . . .                        | 4  |
| auto . . . . .                               | 5  |
| backward_error . . . . .                     | 5  |
| both_ends . . . . .                          | 6  |
| center . . . . .                             | 6  |
| certificate . . . . .                        | 7  |
| check_adjoint . . . . .                      | 8  |
| compose . . . . .                            | 8  |
| crossprod_operator . . . . .                 | 9  |
| diagnostics . . . . .                        | 9  |
| eigen_problem . . . . .                      | 10 |
| eigs . . . . .                               | 11 |
| eigs_sym . . . . .                           | 11 |
| eig_full . . . . .                           | 12 |
| eig_partial . . . . .                        | 13 |
| euclidean . . . . .                          | 15 |
| general . . . . .                            | 15 |
| generalized_schur . . . . .                  | 16 |
| generalized_svd . . . . .                    | 17 |
| golub_kahan . . . . .                        | 17 |
| hermitian . . . . .                          | 18 |
| lanczos . . . . .                            | 18 |
| largest . . . . .                            | 19 |
| largest_imaginary . . . . .                  | 19 |
| largest_magnitude . . . . .                  | 20 |
| largest_real . . . . .                       | 20 |
| left_vectors . . . . .                       | 20 |
| linear_operator . . . . .                    | 21 |
| lobpcg . . . . .                             | 22 |
| nearest . . . . .                            | 23 |
| plan_solver . . . . .                        | 23 |
| randomized . . . . .                         | 24 |
| residuals . . . . .                          | 24 |
| right_vectors . . . . .                      | 25 |
| scale_cols . . . . .                         | 25 |
| scale_rows . . . . .                         | 26 |
| shifted_cholesky_preconditioner . . . . .    | 26 |
| shifted_diagonal_preconditioner . . . . .    | 27 |
| shifted_tridiagonal_preconditioner . . . . . | 27 |
| shift_invert . . . . .                       | 28 |
| smallest . . . . .                           | 28 |
| smallest_imaginary . . . . .                 | 29 |
| smallest_magnitude . . . . .                 | 29 |
| smallest_real . . . . .                      | 29 |

|                                         |           |
|-----------------------------------------|-----------|
| <i>adjoint</i>                          | 3         |
| solve.eigencore_eigen_problem . . . . . | 30        |
| solve.eigencore_svd_problem . . . . .   | 31        |
| svds . . . . .                          | 32        |
| svd_partial . . . . .                   | 32        |
| svd_problem . . . . .                   | 34        |
| symmetric_operator . . . . .            | 34        |
| values . . . . .                        | 35        |
| vectors . . . . .                       | 36        |
| <b>Index</b>                            | <b>37</b> |

---

|         |                                     |
|---------|-------------------------------------|
| adjoint | <i>Return the adjoint operator.</i> |
|---------|-------------------------------------|

---

**Description**

Return the adjoint operator.

**Usage**

adjoint(x, ...)

**Arguments**

- x                   Operator-like object.
- ...                 Additional arguments passed to methods.

**Value**

An eigencore\_operator representing the adjoint map.

---

|            |                                                     |
|------------|-----------------------------------------------------|
| alpha_beta | <i>Extract homogeneous generalized coordinates.</i> |
|------------|-----------------------------------------------------|

---

**Description**

Generalized dense-pencil and generalized Schur results store eigenvalues in homogeneous form as alpha / beta; generalized SVD results use the same alpha/beta convention for generalized singular values. alpha\_beta() exposes those coordinates along with the finite/infinite/undefined classification computed by eigencore.

**Usage**

alpha\_beta(x, ...)

**Arguments**

|     |                                                             |
|-----|-------------------------------------------------------------|
| x   | An eigencore result with homogeneous alpha and beta fields. |
| ... | Reserved for future methods.                                |

**Value**

A list containing alpha, beta, and any available values, classification, finite, infinite, and undefined fields. Results that record how the finite/infinite/undefined labels were decided also include a classification\_policy list with the policy name, the tolerance, the per-coordinate zero thresholds, and the pencil norms used for norm-scaled classification.

**Examples**

```
A <- diag(c(2, 3, 0))
B <- diag(c(1, 0, 0))
fit <- eig_full(A, B = B, structure = general())
alpha_beta(fit)$classification
```

---

as\_operator

---

Convert an object to an eigencore operator.

---

**Description**

Convert an object to an eigencore operator.

**Usage**

```
as_operator(x, ...)
```

**Arguments**

|     |                                         |
|-----|-----------------------------------------|
| x   | Object to convert.                      |
| ... | Additional arguments passed to methods. |

**Value**

An eigencore\_operator representation of x.

**Examples**

```
op <- as_operator(diag(c(3, 2, 1)))
op$dim
op$structure$kind
```

---

|      |                                 |
|------|---------------------------------|
| auto | <i>Automatic solver choice.</i> |
|------|---------------------------------|

---

**Description**

Automatic solver choice.

**Usage**

auto()

**Value**

An eigencore\_method descriptor that lets the planner choose a solver based on problem structure.

---

|                |                                            |
|----------------|--------------------------------------------|
| backward_error | <i>Extract backward-error diagnostics.</i> |
|----------------|--------------------------------------------|

---

**Description**

Extract backward-error diagnostics.

**Usage**

backward\_error(x, ...)

**Arguments**

|     |                              |
|-----|------------------------------|
| x   | An eigencore result object.  |
| ... | Reserved for future methods. |

**Value**

A numeric vector of per-pair or per-triplet backward-error estimates.

---

|           |                                    |
|-----------|------------------------------------|
| both_ends | <i>Target both algebraic ends.</i> |
|-----------|------------------------------------|

---

**Description**

Target both algebraic ends.

**Usage**

```
both_ends(k_low, k_high)
```

**Arguments**

|        |                                                             |
|--------|-------------------------------------------------------------|
| k_low  | Number of values to select from the smallest algebraic end. |
| k_high | Number of values to select from the largest algebraic end.  |

**Value**

An eigencore\_target descriptor selecting both algebraic ends (ARPACK BE).

---

|        |                                               |
|--------|-----------------------------------------------|
| center | <i>Center an operator by rows or columns.</i> |
|--------|-----------------------------------------------|

---

**Description**

Center an operator by rows or columns.

**Usage**

```
center(
  A,
  rows = FALSE,
  columns = TRUE,
  row_means = NULL,
  col_means = NULL,
  name = NULL
)
```

**Arguments**

|           |                                                                                                            |
|-----------|------------------------------------------------------------------------------------------------------------|
| A         | Operator-like object.                                                                                      |
| rows      | Whether to subtract row means.                                                                             |
| columns   | Whether to subtract column means.                                                                          |
| row_means | Optional row means. Required for matrix-free row centering when they cannot be derived without densifying. |

|           |                                                                                                                  |
|-----------|------------------------------------------------------------------------------------------------------------------|
| col_means | Optional column means. Required for matrix-free column centering when they cannot be derived without densifying. |
| name      | Optional label for the centered operator.                                                                        |

**Value**

An eigencore\_operator representing the centered linear map.

---

|             |                                      |
|-------------|--------------------------------------|
| certificate | <i>Extract a result certificate.</i> |
|-------------|--------------------------------------|

---

**Description**

Extract a result certificate.

**Usage**

```
certificate(x, ...)
```

**Arguments**

|     |                              |
|-----|------------------------------|
| x   | An eigencore result object.  |
| ... | Reserved for future methods. |

**Value**

The eigencore\_certificate object stored on x, or NULL if the result does not carry a certificate field.

**Examples**

```
fit <- eig_partial(diag(c(3, 2, 1)), k = 1, target = largest())
cert <- certificate(fit)
cert$passed
cert$max_residual
```

---

|               |                                            |
|---------------|--------------------------------------------|
| check_adjoint | <i>Check an operator adjoint identity.</i> |
|---------------|--------------------------------------------|

---

**Description**

Check an operator adjoint identity.

**Usage**

```
check_adjoint(A, trials = 20, tol = 1e-12, seed = NULL)
```

**Arguments**

|        |                                                     |
|--------|-----------------------------------------------------|
| A      | Operator-like object.                               |
| trials | Number of random block trials.                      |
| tol    | Relative tolerance for each adjoint identity check. |
| seed   | Optional random seed for reproducible trials.       |

**Value**

An eigencore\_adjoint\_check list with pass/fail status, tolerance, maximum relative error, per-trial errors, and trial count.

---

|         |                               |
|---------|-------------------------------|
| compose | <i>Compose two operators.</i> |
|---------|-------------------------------|

---

**Description**

Compose two operators.

**Usage**

```
compose(A, B, name = NULL)
```

**Arguments**

|      |                                           |
|------|-------------------------------------------|
| A    | Left operator-like object.                |
| B    | Right operator-like object.               |
| name | Optional label for the composed operator. |

**Value**

An eigencore\_operator representing the composition  $A \circ B$ .

---

|                    |                                |
|--------------------|--------------------------------|
| crossprod_operator | Create $A^* A$ as an operator. |
|--------------------|--------------------------------|

---

**Description**

Create  $A^* A$  as an operator.

**Usage**

```
crossprod_operator(A, name = NULL)
```

**Arguments**

|      |                                                      |
|------|------------------------------------------------------|
| A    | Operator-like object with an adjoint implementation. |
| name | Optional label for the cross-product operator.       |

**Value**

A Hermitian eigencore\_operator representing  $A^* A$ .

---

|             |                      |
|-------------|----------------------|
| diagnostics | Extract diagnostics. |
|-------------|----------------------|

---

**Description**

Extract diagnostics.

**Usage**

```
diagnostics(x, ...)
```

**Arguments**

|     |                              |
|-----|------------------------------|
| x   | An eigencore result object.  |
| ... | Reserved for future methods. |

**Value**

A named list of diagnostic fields, including residuals, backward errors, orthogonality diagnostics, iteration counts, method/plan metadata, warnings, and any available left-eigenvector diagnostics.

**Examples**

```
fit <- eig_partial(diag(c(3, 2, 1)), k = 1, target = largest())
d <- diagnostics(fit)
d$nconv
d$method
```

---

|               |                                |
|---------------|--------------------------------|
| eigen_problem | <i>Define an eigenproblem.</i> |
|---------------|--------------------------------|

---

## Description

Define an eigenproblem.

## Usage

```
eigen_problem(
  A,
  metric = NULL,
  structure = NULL,
  target = largest(),
  transform = NULL
)
```

## Arguments

|                        |                                                                    |
|------------------------|--------------------------------------------------------------------|
| <code>A</code>         | Matrix or operator defining the linear map.                        |
| <code>metric</code>    | Optional metric operator for generalized eigenproblems.            |
| <code>structure</code> | Optional structure descriptor; defaults to the operator structure. |
| <code>target</code>    | Eigencore target descriptor.                                       |
| <code>transform</code> | Optional transform method such as <a href="#">shift_invert()</a> . |

## Value

An `eigencore_eigen_problem` object containing the operator, optional metric, structure, target, and transform metadata consumed by [plan\\_solver\(\)](#) and [solve\(\)](#).

## Examples

```
A <- diag(c(4, 3, 2, 1))
P <- eigen_problem(A, target = largest())
fit <- solve(P, k = 2)
values(fit)
```

---

|      |                                        |
|------|----------------------------------------|
| eigs | <i>RSpectra-compatible eigen shim.</i> |
|------|----------------------------------------|

---

**Description**

RSpectra-compatible eigen shim.

**Usage**

```
eigs(A, k, which = "LM", opts = list(), ...)
```

**Arguments**

|       |                                                                                                    |
|-------|----------------------------------------------------------------------------------------------------|
| A     | Matrix or eigencore operator.                                                                      |
| k     | Number of eigenpairs to compute.                                                                   |
| which | RSpectra-style target selector.                                                                    |
| opts  | Compatibility options list; currently accepted for API compatibility and not interpreted directly. |
| ...   | Additional arguments passed to <a href="#">eig_partial()</a> .                                     |

**Value**

A list compatible with `RSpectra::eigs()`, including values, vectors, convergence counts, operation counts, certificate diagnostics, and left/right vector fields when available.

**Examples**

```
A <- diag(c(5, 4, 3, 2, 1))
A[1, 2] <- 0.5
res <- eigs(A, k = 2, which = "LM")
res$values
```

---

|          |                                                  |
|----------|--------------------------------------------------|
| eigs_sym | <i>RSpectra-compatible symmetric eigen shim.</i> |
|----------|--------------------------------------------------|

---

**Description**

RSpectra-compatible symmetric eigen shim.

**Usage**

```
eigs_sym(A, k, which = "LA", opts = list(), ...)
```

**Arguments**

|       |                                                                                                    |
|-------|----------------------------------------------------------------------------------------------------|
| A     | Matrix or eigencore operator.                                                                      |
| k     | Number of eigenpairs to compute.                                                                   |
| which | RSpectra-style target selector.                                                                    |
| opts  | Compatibility options list; currently accepted for API compatibility and not interpreted directly. |
| ...   | Additional arguments passed to <code>solve.eigencore_eigen_problem()</code> .                      |

**Value**

A list compatible with `RSpectra::eigs_sym()`, including values, vectors, convergence counts, operation counts, certificate diagnostics, and eigencore diagnostics.

**Examples**

```
A <- diag(c(5, 4, 3, 2, 1))
res <- eigs_sym(A, k = 2, which = "LA")
res$values
```

---

eig\_full

---

*Compute a full dense eigendecomposition*


---

**Description**

`eig_full()` is the dense/full eigencore surface for standard and generalized eigenproblems. Sparse and operator inputs are not silently densified.

**Usage**

```
eig_full(
  A,
  B = NULL,
  structure = NULL,
  vectors = TRUE,
  tol = 1e-08,
  allow_dense_fallback = c("auto", "never", "always"),
  ...
)
```

**Arguments**

|           |                                                                                                                          |
|-----------|--------------------------------------------------------------------------------------------------------------------------|
| A         | Base dense square matrix.                                                                                                |
| B         | Optional base dense square matrix for generalized problems.                                                              |
| structure | Optional structure descriptor. Use <code>general()</code> to force the general-pencil path for dense generalized inputs. |

|                      |                                                                                                                                                            |
|----------------------|------------------------------------------------------------------------------------------------------------------------------------------------------------|
| vectors              | Whether to return right eigenvectors.                                                                                                                      |
| tol                  | Certification tolerance.                                                                                                                                   |
| allow_dense_fallback | Reserved dense fallback policy. Sparse/operator inputs still fail unless a future issue explicitly opens an opt-in dense fallback contract for eig_full(). |
| ...                  | Reserved for future options.                                                                                                                               |

### Value

An eigencore\_eigen\_result. Dense general-pencil results additionally carry alpha, beta, classification, classification\_policy, left\_vectors (left generalized eigenvectors satisfying  $w^H A = \lambda w^H B$ ), and conditioning. For real pencils the decomposition runs through the expert LAPACK driver DGGEVX with balancing, so conditioning contains reciprocal condition numbers rconde/rcondv and the balanced pencil norms abnrm/bbnrm. Complex pencils use ZGGEV (R's bundled LAPACK subset has no ZGGEVX), so they return left vectors but conditioning\$available is FALSE.

### Examples

```
A <- diag(c(1, 4, 9))
B <- diag(c(1, 2, 3))
fit <- eig_full(A, B = B)
values(fit)
certificate(fit)$passed

# Force the dense general-pencil path when alpha/beta diagnostics matter.
pencil <- eig_full(A, B = B, structure = general())
pencil$alpha
pencil$beta
pencil$classification
```

---

|             |                                              |
|-------------|----------------------------------------------|
| eig_partial | <i>Compute a partial eigendecomposition.</i> |
|-------------|----------------------------------------------|

---

### Description

Compute a partial eigendecomposition.

### Usage

```
eig_partial(
  A,
  k,
  target = largest(),
  B = NULL,
  method = auto(),
  tol = 1e-08,
  maxit = NULL,
  vectors = TRUE,
```

```

    seed = NULL,
    certify = TRUE,
    allow_dense_fallback = c("auto", "never", "always")
  )

```

## Arguments

|                                   |                                                              |
|-----------------------------------|--------------------------------------------------------------|
| <code>A</code>                    | Matrix or eigencore operator.                                |
| <code>k</code>                    | Number of eigenpairs to compute.                             |
| <code>target</code>               | Eigencore eigenvalue target descriptor.                      |
| <code>B</code>                    | Optional metric matrix or operator for generalized problems. |
| <code>method</code>               | Solver method descriptor.                                    |
| <code>tol</code>                  | Convergence and certification tolerance.                     |
| <code>maxit</code>                | Optional iteration limit.                                    |
| <code>vectors</code>              | Whether to compute vectors.                                  |
| <code>seed</code>                 | Optional random seed for stochastic solver components.       |
| <code>certify</code>              | Whether to compute certification diagnostics.                |
| <code>allow_dense_fallback</code> | Dense fallback policy.                                       |

## Value

An `eigencore_eigen_result` containing computed values, optional vectors, certificate diagnostics, method/plan metadata, and convergence diagnostics.

## Examples

```

A <- diag(c(5, 4, 3, 2, 1))
A[1, 2] <- A[2, 1] <- 0.1
fit <- eig_partial(A, k = 2, target = largest())
values(fit)
certificate(fit)$passed

# Generalized SPD problem A x = lambda B x
B <- diag(c(2, 1, 1, 1, 1))
gfit <- eig_partial(A, B = B, k = 2, target = smallest())
values(gfit)

```

---

|           |                                           |
|-----------|-------------------------------------------|
| euclidean | <i>Euclidean vector space descriptor.</i> |
|-----------|-------------------------------------------|

---

**Description**

Euclidean vector space descriptor.

**Usage**

```
euclidean(dim, dtype = "double")
```

**Arguments**

|       |                                        |
|-------|----------------------------------------|
| dim   | Dimension of the space.                |
| dtype | Scalar type (currently only "double"). |

**Value**

An eigencore\_space descriptor for the Euclidean space  $\mathbb{R}^{\text{dim}}$  or  $\mathbb{C}^{\text{dim}}$ .

---

|         |                                               |
|---------|-----------------------------------------------|
| general | <i>General operator structure descriptor.</i> |
|---------|-----------------------------------------------|

---

**Description**

General operator structure descriptor.

**Usage**

```
general()
```

**Value**

An eigencore\_structure descriptor for general operators.

---

|                   |                                                        |
|-------------------|--------------------------------------------------------|
| generalized_schur | <i>Compute a dense generalized Schur decomposition</i> |
|-------------------|--------------------------------------------------------|

---

## Description

`generalized_schur()` is `eigencore`'s dense QZ surface for general matrix pencils  $A x = \lambda B x$ . It computes the generalized Schur pair  $S, T$  and, when requested, left/right Schur vectors  $Q, Z$  such that  $A = Q S Z^*$  and  $B = Q T Z^*$  for complex inputs, with transpose replacing conjugate-transpose for real inputs. Sparse and operator inputs are not silently densified.

## Usage

```
generalized_schur(A, B, sort = NULL, vectors = TRUE, ...)
```

## Arguments

|                      |                                                                                                                                                                                                                                                                                                                                              |
|----------------------|----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| <code>A</code>       | Base dense square matrix.                                                                                                                                                                                                                                                                                                                    |
| <code>B</code>       | Base dense square matrix with the same dimension as <code>A</code> .                                                                                                                                                                                                                                                                         |
| <code>sort</code>    | Optional LAPACK sorting class. Use <code>NULL</code> or <code>"none"</code> for no sorting, <code>"finite"</code> to move finite generalized eigenvalues first, <code>"infinite"</code> to move beta-zero nonzero-alpha eigenvalues first. Custom predicates and undefined alpha-zero/beta-zero sorting are not part of the public contract. |
| <code>vectors</code> | Whether to compute Schur vectors $Q$ and $Z$ .                                                                                                                                                                                                                                                                                               |
| <code>...</code>     | Reserved for future options.                                                                                                                                                                                                                                                                                                                 |

## Value

A classed generalized Schur result with fields `S`, `T`, `Q`, `Z`, `alpha`, `beta`, `values`, `classification`, `sdim`, `method`, `plan`, and `certificate`.

## Examples

```
A <- matrix(c(0, -1, 1, 0), 2, 2)
B <- diag(2)
qz <- generalized_schur(A, B)
values(qz)

pencil <- generalized_schur(diag(c(2, 3, 0)), diag(c(1, 0, 0)),
                           sort = "infinite")
pencil$classification
```

---

|                 |                                                                 |
|-----------------|-----------------------------------------------------------------|
| generalized_svd | <i>Compute a dense generalized singular value decomposition</i> |
|-----------------|-----------------------------------------------------------------|

---

### Description

`generalized_svd()` is eigencore's dense GSVD compatibility surface for matrix pairs with the same number of columns. The current native path uses LAPACK `dggsvd` through R's native LAPACK interface, so it requires a linked LAPACK that still provides that deprecated routine. Sparse/operator inputs are not silently densified, and complex GSVD remains explicit future scope until a complex GSVD driver is available through the eigencore native layer.

### Usage

```
generalized_svd(A, B, tol = 1e-08, ...)
```

### Arguments

|     |                                                                               |
|-----|-------------------------------------------------------------------------------|
| A   | Base dense real matrix with $m$ rows and $n$ columns.                         |
| B   | Base dense real matrix with $p$ rows and $n$ columns.                         |
| tol | Finite non-negative reconstruction and orthogonality certification tolerance. |
| ... | Reserved for future options.                                                  |

### Value

An `eigencore_gsvd_result` with fields `alpha`, `beta`, `values`, `classification`, `U`, `V`, `Q`, `D1`, `D2`, `R`, `zero_R`, `A_factor`, `B_factor`, `k`, `l`, `rank`, `method`, `plan`, and `certificate`.

### Examples

```
A <- matrix(c(1, 2, 3, 3, 2, 1), nrow = 2, byrow = TRUE)
B <- matrix(1:9, nrow = 3)
fit <- generalized_svd(A, B)
alpha_beta(fit)$values
certificate(fit)$passed
```

---

|             |                                                         |
|-------------|---------------------------------------------------------|
| golub_kahan | <i>Golub-Kahan bidiagonalization method descriptor.</i> |
|-------------|---------------------------------------------------------|

---

### Description

Golub-Kahan bidiagonalization method descriptor.

### Usage

```
golub_kahan(max_subspace = NULL, reorthogonalize = TRUE)
```

**Arguments**

max\_subspace    Optional maximum Krylov subspace size.

reorthogonalize    Whether to apply full two-sided reorthogonalization. FALSE selects the native one-sided small-side policy where supported, with final acceptance still controlled by the exact two-sided certificate.

**Value**

An eigencore\_method descriptor selecting Golub-Kahan bidiagonalization.

---

|           |                                                           |
|-----------|-----------------------------------------------------------|
| hermitian | <i>Hermitian/symmetric operator structure descriptor.</i> |
|-----------|-----------------------------------------------------------|

---

**Description**

Hermitian/symmetric operator structure descriptor.

**Usage**

```
hermitian()
```

**Value**

An eigencore\_structure descriptor marking an operator as Hermitian / symmetric.

---

|         |                                             |
|---------|---------------------------------------------|
| lanczos | <i>Hermitian Lanczos method descriptor.</i> |
|---------|---------------------------------------------|

---

**Description**

Hermitian Lanczos method descriptor.

**Usage**

```
lanczos(
  max_subspace = NULL,
  max_restarts = NULL,
  block = 1L,
  reorthogonalize = TRUE
)
```

**Arguments**

|                              |                                                                                                                                                                                 |
|------------------------------|---------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| <code>max_subspace</code>    | Optional maximum active Krylov subspace size $m$ . Must be at least $k + 1$ . The native thick-restart path keeps the active basis bounded by this value across restart cycles. |
| <code>max_restarts</code>    | Optional non-negative integer giving the maximum number of thick-restart cycles allowed before stopping with whatever has converged. Default 100L.                              |
| <code>block</code>           | Native block size. 1L selects the scalar thick-restart path; values greater than one select the native block Krylov prototype where supported.                                  |
| <code>reorthogonalize</code> | Whether to apply full reorthogonalization. The native path always reorthogonalizes (DGKS x2) and ignores this flag; it is preserved for the R reference solver's public API.    |

**Value**

An `eigencore_method` descriptor selecting Lanczos iteration.

---

|                      |                                             |
|----------------------|---------------------------------------------|
| <code>largest</code> | <i>Target the largest algebraic values.</i> |
|----------------------|---------------------------------------------|

---

**Description**

Target the largest algebraic values.

**Usage**

```
largest()
```

**Value**

An `eigencore_target` descriptor selecting the largest algebraic eigenvalues or singular values.

---

|                                |                                           |
|--------------------------------|-------------------------------------------|
| <code>largest_imaginary</code> | <i>Target the largest imaginary part.</i> |
|--------------------------------|-------------------------------------------|

---

**Description**

Target the largest imaginary part.

**Usage**

```
largest_imaginary()
```

**Value**

An `eigencore_target` descriptor selecting values by largest  $\text{Im}(x)$  (ARPACK LI).

---

|                   |                                                |
|-------------------|------------------------------------------------|
| largest_magnitude | <i>Target the largest values by magnitude.</i> |
|-------------------|------------------------------------------------|

---

**Description**

Target the largest values by magnitude.

**Usage**

```
largest_magnitude()
```

**Value**

An eigencore\_target descriptor selecting values with the largest modulus (ARPACK LM).

---

|              |                                      |
|--------------|--------------------------------------|
| largest_real | <i>Target the largest real part.</i> |
|--------------|--------------------------------------|

---

**Description**

Target the largest real part.

**Usage**

```
largest_real()
```

**Value**

An eigencore\_target descriptor selecting values by largest  $\text{Re}(x)$  (ARPACK LR).

---

|              |                                                            |
|--------------|------------------------------------------------------------|
| left_vectors | <i>Extract left singular vectors or left eigenvectors.</i> |
|--------------|------------------------------------------------------------|

---

**Description**

For SVD results this returns the left singular vectors  $U$ . For nonsymmetric and dense general-pencil eigen results this returns left eigenvectors when the solver computed them (for example, the dense general-pencil `eig_full()` path, which computes left generalized eigenvectors satisfying  $w^H A = \lambda w^H B$ ).

**Usage**

```
left_vectors(x, ...)
```

**Arguments**

`x`                      An eigencore SVD or eigen result object.

`...`                    Reserved for future methods.

**Value**

A matrix of left singular vectors or left eigenvectors, or NULL when the result does not contain a left-vector field.

---

|                              |                                               |
|------------------------------|-----------------------------------------------|
| <code>linear_operator</code> | <i>Create a block-native linear operator.</i> |
|------------------------------|-----------------------------------------------|

---

**Description**

Create a block-native linear operator.

**Usage**

```
linear_operator(
  dim,
  apply,
  apply_adjoint = NULL,
  dtype = "double",
  structure = general(),
  name = NULL,
  metadata = list()
)
```

**Arguments**

`dim`                    Integer vector of length two giving row and column dimensions.

`apply`                 Function implementing block multiplication by the operator.

`apply_adjoint`        Optional function implementing block multiplication by the adjoint operator.

`dtype`                 Scalar character type label, currently "double" or "complex".

`structure`            Eigencore structure descriptor such as `general()` or `hermitian()`.

`name`                  Optional operator label used in plans and diagnostics.

`metadata`             Optional list of implementation metadata.

**Value**

An `eigencore_operator` list containing dimensions, apply callbacks, scalar type, structure metadata, a display name, and implementation metadata.

**Examples**

```

A <- diag(c(3, 2, 1))
op <- linear_operator(
  dim = dim(A),
  apply = function(X, alpha = 1, beta = 0, Y = NULL) {
    Z <- alpha * (A %*% X)
    if (is.null(Y) || beta == 0) Z else Z + beta * Y
  },
  structure = hermitian(),
  metadata = list(frobenius_norm = sqrt(sum(A^2)))
)
fit <- eig_partial(op, k = 1, target = largest())
values(fit)

```

lobpcg

*LOBPCG method descriptor.***Description**

LOBPCG method descriptor.

**Usage**

```
lobpcg(maxit = 200L, preconditioner = NULL, constraints = NULL)
```

**Arguments**

|                |                                                                                                                                                                                                                                                             |
|----------------|-------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| maxit          | Maximum LOBPCG iterations.                                                                                                                                                                                                                                  |
| preconditioner | Optional function taking a residual block and returning a preconditioned block with the same dimensions.                                                                                                                                                    |
| constraints    | Optional matrix whose columns span a subspace to deflate. Iterates are kept orthogonal to this subspace in the Euclidean or generalized B inner product. Native constrained LOBPCG is not promoted yet; constrained problems use the honest reference path. |

**Value**

An eigencore\_method descriptor selecting LOBPCG. Built-in standard Hermitian dense/CSC operators may use a native prototype; unsupported cases route to the reference prototype.

---

|         |                                       |
|---------|---------------------------------------|
| nearest | <i>Target values nearest a shift.</i> |
|---------|---------------------------------------|

---

**Description**

Target values nearest a shift.

**Usage**

```
nearest(sigma)
```

**Arguments**

sigma            Numeric shift used to rank values by distance  $|x - \text{sigma}|$ .

**Value**

An eigencore\_target descriptor for nearest-to-sigma selection.

---

|             |                                     |
|-------------|-------------------------------------|
| plan_solver | <i>Plan a solver for a problem.</i> |
|-------------|-------------------------------------|

---

**Description**

Plan a solver for a problem.

**Usage**

```
plan_solver(problem, ...)
```

**Arguments**

problem            Eigencore eigen or SVD problem object.  
 ...                Additional planning arguments passed to methods.

**Value**

An eigencore\_plan list describing the requested problem, chosen method label, target, planner reasons, fallback label, and control metadata used by solver dispatch.

**Examples**

```
A <- diag(c(4, 3, 2, 1))
plan <- plan_solver(eigen_problem(A), k = 2)
plan$method
plan$reasons
```

---

|            |                                          |
|------------|------------------------------------------|
| randomized | <i>Randomized SVD method descriptor.</i> |
|------------|------------------------------------------|

---

### Description

Randomized SVD method descriptor.

### Usage

```
randomized(
    oversample = 10,
    n_iter = 2,
    block = NULL,
    normalizer = c("qr", "lu", "none"),
    refine = TRUE
)
```

### Arguments

|            |                                                    |
|------------|----------------------------------------------------|
| oversample | Number of extra samples beyond the requested rank. |
| n_iter     | Number of subspace-iteration refinement passes.    |
| block      | Optional block size.                               |
| normalizer | Basis normalizer to use ("qr", "lu", or "none").   |
| refine     | Whether to refine with a certified Lanczos pass.   |

### Value

An eigencore\_method descriptor selecting randomized SVD.

---

|           |                                      |
|-----------|--------------------------------------|
| residuals | <i>Extract residual diagnostics.</i> |
|-----------|--------------------------------------|

---

### Description

Methods for the `stats::residuals()` generic: return the per-pair (or per-triplet) residual norms stored in an eigencore result or certificate.

### Usage

```
## S3 method for class 'eigencore_eigen_result'
residuals(object, ...)

## S3 method for class 'eigencore_svd_result'
residuals(object, ...)

## S3 method for class 'eigencore_certificate'
residuals(object, ...)
```

**Arguments**

|        |                                            |
|--------|--------------------------------------------|
| object | An eigencore result or certificate object. |
| ...    | Reserved for future methods.               |

---

|               |                                        |
|---------------|----------------------------------------|
| right_vectors | <i>Extract right singular vectors.</i> |
|---------------|----------------------------------------|

---

**Description**

Extract right singular vectors.

**Usage**

```
right_vectors(x, ...)
```

**Arguments**

|     |                                                       |
|-----|-------------------------------------------------------|
| x   | An eigencore SVD or nonsymmetric eigen result object. |
| ... | Reserved for future methods.                          |

**Value**

A matrix of right singular vectors or right eigenvectors, or NULL when the result does not contain a right-vector field.

---

|            |                                |
|------------|--------------------------------|
| scale_cols | <i>Scale operator columns.</i> |
|------------|--------------------------------|

---

**Description**

Scale operator columns.

**Usage**

```
scale_cols(A, weights, name = NULL)
```

**Arguments**

|         |                                         |
|---------|-----------------------------------------|
| A       | Operator-like object.                   |
| weights | Numeric vector of column weights.       |
| name    | Optional label for the scaled operator. |

**Value**

An eigencore\_operator representing column-wise right scaling of A.

---

|            |                      |
|------------|----------------------|
| scale_rows | Scale operator rows. |
|------------|----------------------|

---

**Description**

Scale operator rows.

**Usage**

```
scale_rows(A, weights, name = NULL)
```

**Arguments**

- A                   Operator-like object.
- weights            Numeric vector of row weights.
- name               Optional label for the scaled operator.

**Value**

An eigencore\_operator representing row-wise left scaling of A.

---

|                                 |                                  |
|---------------------------------|----------------------------------|
| shifted_cholesky_preconditioner | Shifted Cholesky preconditioner. |
|---------------------------------|----------------------------------|

---

**Description**

Shifted Cholesky preconditioner.

**Usage**

```
shifted_cholesky_preconditioner(A, shift = 0)
```

**Arguments**

- A                   Symmetric positive semidefinite or positive definite matrix.
- shift               Non-negative diagonal shift added before factorization.

**Value**

A typed preconditioner function mapping residual blocks to preconditioned blocks.

---

shifted\_diagonal\_preconditioner  
*Shifted diagonal preconditioner.*

---

**Description**

Shifted diagonal preconditioner.

**Usage**

```
shifted_diagonal_preconditioner(A, shift = 0)
```

**Arguments**

|       |                                                                    |
|-------|--------------------------------------------------------------------|
| A     | Diagonal matrix or numeric vector containing the diagonal entries. |
| shift | Non-negative diagonal shift added before inversion.                |

**Value**

A typed native-backed preconditioner function mapping residual blocks to preconditioned blocks.

---

shifted\_tridiagonal\_preconditioner  
*Shifted tridiagonal preconditioner.*

---

**Description**

Shifted tridiagonal preconditioner.

**Usage**

```
shifted_tridiagonal_preconditioner(A, shift = 0)
```

**Arguments**

|       |                                                              |
|-------|--------------------------------------------------------------|
| A     | Real symmetric tridiagonal matrix.                           |
| shift | Non-negative diagonal shift added to the tridiagonal system. |

**Value**

A typed preconditioner function mapping residual blocks to preconditioned blocks.

---

|              |                                        |
|--------------|----------------------------------------|
| shift_invert | <i>Shift-invert method descriptor.</i> |
|--------------|----------------------------------------|

---

**Description**

Shift-invert method descriptor.

**Usage**

```
shift_invert(sigma, solve = NULL, factorization = NULL)
```

**Arguments**

|               |                                                              |
|---------------|--------------------------------------------------------------|
| sigma         | Shift value sigma.                                           |
| solve         | Optional user-supplied solve operator for $(A - \sigma B)$ . |
| factorization | Optional precomputed factorization handle.                   |

**Value**

An eigencore\_method descriptor selecting shift-invert.

---

|          |                                              |
|----------|----------------------------------------------|
| smallest | <i>Target the smallest algebraic values.</i> |
|----------|----------------------------------------------|

---

**Description**

Target the smallest algebraic values.

**Usage**

```
smallest()
```

**Value**

An eigencore\_target descriptor selecting the smallest algebraic eigenvalues or singular values.

---

|                    |                                            |
|--------------------|--------------------------------------------|
| smallest_imaginary | <i>Target the smallest imaginary part.</i> |
|--------------------|--------------------------------------------|

---

**Description**

Target the smallest imaginary part.

**Usage**

smallest\_imaginary()

**Value**

An eigencore\_target descriptor selecting values by smallest  $\text{Im}(x)$  (ARPACK SI).

---

|                    |                                                 |
|--------------------|-------------------------------------------------|
| smallest_magnitude | <i>Target the smallest values by magnitude.</i> |
|--------------------|-------------------------------------------------|

---

**Description**

Target the smallest values by magnitude.

**Usage**

smallest\_magnitude()

**Value**

An eigencore\_target descriptor selecting values with the smallest modulus (ARPACK SM).

---

|               |                                       |
|---------------|---------------------------------------|
| smallest_real | <i>Target the smallest real part.</i> |
|---------------|---------------------------------------|

---

**Description**

Target the smallest real part.

**Usage**

smallest\_real()

**Value**

An eigencore\_target descriptor selecting values by smallest  $\text{Re}(x)$  (ARPACK SR).

---

```
solve.eigencore_eigen_problem
```

*Solve a planned eigenproblem.*

---

### Description

S3 method that runs the planned solver for an eigenproblem built by `eigen_problem()`. Most users call `eig_partial()`, which constructs the problem and dispatches here; call `solve()` directly when you want to build a problem once and reuse or inspect it. Returns a certified partial eigendecomposition.

### Usage

```
## S3 method for class 'eigencore_eigen_problem'
solve(
  a,
  b,
  k,
  method = auto(),
  tol = 1e-08,
  maxit = NULL,
  vectors = TRUE,
  certify = TRUE,
  allow_dense_fallback = c("auto", "never", "always"),
  ...
)
```

### Arguments

|                                   |                                                                           |
|-----------------------------------|---------------------------------------------------------------------------|
| <code>a</code>                    | Eigencore eigen problem object.                                           |
| <code>b</code>                    | Unused second argument reserved by the base <code>solve()</code> generic. |
| <code>k</code>                    | Number of eigenpairs to compute.                                          |
| <code>method</code>               | Solver method descriptor.                                                 |
| <code>tol</code>                  | Convergence and certification tolerance.                                  |
| <code>maxit</code>                | Optional iteration limit.                                                 |
| <code>vectors</code>              | Whether to compute vectors.                                               |
| <code>certify</code>              | Whether to compute certification diagnostics.                             |
| <code>allow_dense_fallback</code> | Dense fallback policy.                                                    |
| <code>...</code>                  | Reserved for future solver options.                                       |

### Value

An `eigencore_eigen_result`.

---

solve.eigencore\_svd\_problem

*Solve a planned SVD problem.*


---

## Description

S3 method that runs the planned solver for an SVD problem built by `svd_problem()`. Most users call `svd_partial()`, which constructs the problem and dispatches here; call `solve()` directly when you want to build a problem once and reuse or inspect it. Returns a certified partial singular-value decomposition.

## Usage

```
## S3 method for class 'eigencore_svd_problem'
solve(
  a,
  b,
  rank,
  method = auto(),
  tol = 1e-08,
  vectors = c("both", "left", "right", "none"),
  certify = TRUE,
  allow_dense_fallback = c("auto", "never", "always"),
  ...
)
```

## Arguments

|                                   |                                                                           |
|-----------------------------------|---------------------------------------------------------------------------|
| <code>a</code>                    | Eigencore SVD problem object.                                             |
| <code>b</code>                    | Unused second argument reserved by the base <code>solve()</code> generic. |
| <code>rank</code>                 | Number of singular values to compute.                                     |
| <code>method</code>               | Solver method descriptor.                                                 |
| <code>tol</code>                  | Convergence and certification tolerance.                                  |
| <code>vectors</code>              | Which singular-vector sides to compute.                                   |
| <code>certify</code>              | Whether to compute certification diagnostics.                             |
| <code>allow_dense_fallback</code> | Dense fallback policy.                                                    |
| <code>...</code>                  | Reserved for future solver options.                                       |

## Value

An `eigencore_svd_result`.

---

|      |                                      |
|------|--------------------------------------|
| svds | <i>RSpectra-compatible SVD shim.</i> |
|------|--------------------------------------|

---

### Description

RSpectra-compatible SVD shim.

### Usage

```
svds(A, k, nu = k, nv = k, opts = list(), ...)
```

### Arguments

|      |                                                                                                    |
|------|----------------------------------------------------------------------------------------------------|
| A    | Matrix or eigencore operator.                                                                      |
| k    | Number of singular values to compute.                                                              |
| nu   | Number of left singular vectors requested.                                                         |
| nv   | Number of right singular vectors requested.                                                        |
| opts | Compatibility options list; currently accepted for API compatibility and not interpreted directly. |
| ...  | Additional arguments passed to <a href="#">svd_partial()</a> .                                     |

### Value

A list compatible with `RSpectra::svds()`, including `d`, optional `u` and `v`, convergence counts, operation counts, certificate diagnostics, and eigencore diagnostics.

### Examples

```
set.seed(1)
X <- matrix(rnorm(60), 10, 6)
res <- svds(X, k = 2)
res$d
```

---

|             |                                                        |
|-------------|--------------------------------------------------------|
| svd_partial | <i>Compute a partial singular-value decomposition.</i> |
|-------------|--------------------------------------------------------|

---

### Description

Compute a partial singular-value decomposition.

**Usage**

```
svd_partial(
  A,
  rank,
  target = largest(),
  method = auto(),
  tol = 1e-08,
  vectors = c("both", "left", "right", "none"),
  seed = NULL,
  certify = TRUE,
  allow_dense_fallback = c("auto", "never", "always")
)
```

**Arguments**

|                                   |                                                        |
|-----------------------------------|--------------------------------------------------------|
| <code>A</code>                    | Matrix or eigencore operator.                          |
| <code>rank</code>                 | Number of singular values to compute.                  |
| <code>target</code>               | Eigencore singular-value target descriptor.            |
| <code>method</code>               | Solver method descriptor.                              |
| <code>tol</code>                  | Convergence and certification tolerance.               |
| <code>vectors</code>              | Which singular-vector sides to compute.                |
| <code>seed</code>                 | Optional random seed for stochastic solver components. |
| <code>certify</code>              | Whether to compute certification diagnostics.          |
| <code>allow_dense_fallback</code> | Dense fallback policy.                                 |

**Value**

An `eigencore_svd_result` containing singular values, optional left and right singular vectors, certificate diagnostics, method/plan metadata, and convergence diagnostics.

**Examples**

```
set.seed(1)
X <- matrix(rnorm(60), 10, 6)
fit <- svd_partial(X, rank = 3)
values(fit)
certificate(fit)$passed
```

---

|             |                               |
|-------------|-------------------------------|
| svd_problem | <i>Define an SVD problem.</i> |
|-------------|-------------------------------|

---

**Description**

Define an SVD problem.

**Usage**

```
svd_problem(A, domain = NULL, codomain = NULL, target = largest())
```

**Arguments**

|          |                                                         |
|----------|---------------------------------------------------------|
| A        | Matrix or operator defining the rectangular linear map. |
| domain   | Optional domain-space descriptor.                       |
| codomain | Optional codomain-space descriptor.                     |
| target   | Eigencore singular-value target descriptor.             |

**Value**

An eigencore\_svd\_problem object containing the operator, domain and codomain descriptors, and singular-value target consumed by [plan\\_solver\(\)](#) and [solve\(\)](#).

**Examples**

```
set.seed(1)
X <- matrix(rnorm(40), 8, 5)
S <- svd_problem(X, target = largest())
fit <- solve(S, rank = 2)
values(fit)
```

---

|                    |                                                 |
|--------------------|-------------------------------------------------|
| symmetric_operator | <i>Mark an operator as symmetric/Hermitian.</i> |
|--------------------|-------------------------------------------------|

---

**Description**

Mark an operator as symmetric/Hermitian.

**Usage**

```
symmetric_operator(A, validate = TRUE, tol = 1e-10)
```

**Arguments**

|          |                                                                              |
|----------|------------------------------------------------------------------------------|
| A        | Operator-like object.                                                        |
| validate | Whether to check the adjoint identity before marking the operator symmetric. |
| tol      | Relative tolerance for the adjoint check.                                    |

**Value**

An eigencore\_operator with Hermitian structure metadata.

---

|        |                                 |
|--------|---------------------------------|
| values | <i>Extract computed values.</i> |
|--------|---------------------------------|

---

**Description**

Extract computed values.

**Usage**

```
values(x, ...)
```

**Arguments**

|     |                              |
|-----|------------------------------|
| x   | An eigencore result object.  |
| ... | Reserved for future methods. |

**Value**

A numeric or complex vector of computed eigenvalues, singular values, or generalized singular values.

**Examples**

```
fit <- eig_partial(diag(c(3, 2, 1)), k = 2, target = largest())
values(fit)
```

---

|         |                              |
|---------|------------------------------|
| vectors | <i>Extract eigenvectors.</i> |
|---------|------------------------------|

---

**Description**

Extract eigenvectors.

**Usage**

```
vectors(x, ...)
```

**Arguments**

|     |                                   |
|-----|-----------------------------------|
| x   | An eigencore eigen result object. |
| ... | Reserved for future methods.      |

**Value**

A matrix whose columns are computed right eigenvectors, or NULL when vectors were not requested or are unavailable.

**Examples**

```
fit <- eig_partial(diag(c(3, 2, 1)), k = 2, target = largest())  
dim(vectors(fit))
```

# Index

adjoint, [3](#)  
alpha\_beta, [3](#)  
as\_operator, [4](#)  
auto, [5](#)  
  
backward\_error, [5](#)  
both\_ends, [6](#)  
  
center, [6](#)  
certificate, [7](#)  
check\_adjoint, [8](#)  
compose, [8](#)  
crossprod\_operator, [9](#)  
  
diagnostics, [9](#)  
  
eig\_full, [12](#)  
eig\_partial, [13](#)  
eig\_partial(), [11](#), [30](#)  
eigen\_problem, [10](#)  
eigen\_problem(), [30](#)  
eigs, [11](#)  
eigs\_sym, [11](#)  
euclidean, [15](#)  
  
general, [15](#)  
general(), [12](#), [21](#)  
generalized\_schur, [16](#)  
generalized\_svd, [17](#)  
golub\_kahan, [17](#)  
  
hermitian, [18](#)  
hermitian(), [21](#)  
  
lanczos, [18](#)  
largest, [19](#)  
largest\_imaginary, [19](#)  
largest\_magnitude, [20](#)  
largest\_real, [20](#)  
left\_vectors, [20](#)  
linear\_operator, [21](#)  
  
lobpcg, [22](#)  
  
nearest, [23](#)  
  
plan\_solver, [23](#)  
plan\_solver(), [10](#), [34](#)  
  
randomized, [24](#)  
residuals, [24](#)  
right\_vectors, [25](#)  
  
scale\_cols, [25](#)  
scale\_rows, [26](#)  
shift\_invert, [28](#)  
shift\_invert(), [10](#)  
shifted\_cholesky\_preconditioner, [26](#)  
shifted\_diagonal\_preconditioner, [27](#)  
shifted\_tridiagonal\_preconditioner, [27](#)  
smallest, [28](#)  
smallest\_imaginary, [29](#)  
smallest\_magnitude, [29](#)  
smallest\_real, [29](#)  
solve(), [10](#), [30](#), [31](#), [34](#)  
solve.eigencore\_eigen\_problem, [30](#)  
solve.eigencore\_eigen\_problem(), [12](#)  
solve.eigencore\_svd\_problem, [31](#)  
stats::residuals(), [24](#)  
svd\_partial, [32](#)  
svd\_partial(), [31](#), [32](#)  
svd\_problem, [34](#)  
svd\_problem(), [31](#)  
svds, [32](#)  
symmetric\_operator, [34](#)  
  
values, [35](#)  
vectors, [36](#)